

## SCHEME OF COURSEWORK

### Course Details:

|                                       |  |         |         |
|---------------------------------------|--|---------|---------|
| Course Title                          | Discrete Mathematical Structures   |         |         |
| Course Code                           | 15BM1106   | L T P C | 3 0 0 3 |
| Program:                              | B.Tech.  |         |         |
| Specialization:                       | Information Technology   |         |         |
| Semester                              | III Semester   |         |         |
| Prerequisites                         | <ul style="list-style-type: none"><li>• Fundamentals of Set theory</li><li>• Elementary algebra and Calculus</li></ul>           |         |         |
| Courses to which it is a prerequisite | Theory of Computation, Design and analysis of Algorithms, Compiler Design, Principles of Programming Languages, Data Structures. |         |         |

### Course Outcomes (COs): At the end of the Course, Student will be able to:

1. Rewrite mathematical arguments using logical connectives and quantifiers and verify the validity of logical flow of arguments using propositional, predicate logic and truth tables.
2. Identify and give examples of various types of relations and describe various properties of the relations. Classify certain basic algebraic structures and discuss their properties.
3. demonstrate the ability to solve problems using Combinatorics
4. Determine isomorphism of graphs and spanning tree of a given graph using DFS / BFS. Also determine minimal spanning tree of a given graph.
5. Explain fundamental concepts of fuzzy sets and apply them to an expert system.

### PROGRAM OUTCOMES:

A graduate of Information Technology Engineering will be able to

PO1: Apply the knowledge of mathematics, science, engineering fundamentals and principles of Information Technology to solve problems in different domains.

PO2: Analyze a problem, identify and formulate the computing requirements appropriate to its solution.

PO3: Design and develop software components, patterns, processes, Frameworks and applications that meet specifications within the realistic constraints including societal, legal and economic to serve the needs of the society

PO4: Design and conduct experiments, as well as analyze and interpret data PO5: Use appropriate techniques and tools to solve engineering problems.

PO6: Understand the impact of Information technology on environment and the evolution and importance of green computing.

PO7: Analyze the local and global impact of computing on individual as well as on society and incorporate the results into engineering practice.

PO8: Demonstrate professional ethical practices and social responsibilities in global and societal contexts.



## Teaching-Learning and Evaluation

| Week | TOPIC / CONTENTS  | Course Outcomes | Sample questions  | TEACHING-LEARNING STRATEGY | Assessment Method & Schedule                |
|------|---|-----------------|---|----------------------------|---|
| 1    | Statements and notations, connectives, Well formed formulae, Tautologies, Tautological Implications, equivalence of formulas, Duality law and other connectives | CO-I            | Show the following implication with constructing truth table<br>$\neg P \vee Q \Rightarrow P \Rightarrow Q$   | Lecture/ Problem solving   | Assignment (Week 2-4) / Mid-Test 1 (Week 9) |
| 2    | Normal forms, Rules of inference, Consistency of premises and Indirect method of proof.   | CO-I            | Obtain the principal conjunctive normal form and principal disjunctive normal form of<br>$(P \vee R) \wedge (Q \vee P)$                                   | Lecture/ Problem solving   | Assignment (Week 2-4) / Mid-Test 1 (Week 9) |
| 3    | Rules of inference, Consistency of premises and Indirect method of proof. Predicates, the statement function, variables and quantifiers                         | CO-I            | Show that $R \Rightarrow S$ can be derived from the premises<br>$P \Rightarrow (Q \vee S), R \Rightarrow P$<br>Q<br>and                                   | Lecture/ Problem solving   | Assignment (Week 2-4) / Mid-Test 1 (Week 9) |
| 4    | predicate formula, free and bound variables, universe of discourse, inference theory of the predicate calculus  | CO-I            | Show that<br>$\forall x (p(x) \vee q(x)) \Rightarrow \exists x (p(x) \vee q(x))$<br>$\exists x (p(x) \wedge q(x)) \Rightarrow \exists x (p(x) \vee q(x))$ | Lecture/ Problem solving   | Assignment (Week 2-4) / Mid-Test 1 (Week 9) |
| 5    | Relations, properties of binary relations in a set, Relation matrix and Graph of a relation   | CO-II           | If R and S are equivalence relations on the set A, prove that $(R \cap S)$ is an equivalence relation.  | Lecture/ Problem solving   | Mid-Test 1 (Week 9) / Quiz                  |

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|---|--|-------|---|-----------------------------|--------------------------|
| 6 | Partition and covering of a set, equivalence relations, Compatible relation, Composition of binary relations.                                      | CO-II | If $R$ is a Relation in the set of integers defined by $R = \{(x,y) \mid x \text{ and } y \text{ integers and } (x-y) \text{ is divisible by } 5\}$ then prove that $R$ is an equivalence relation. | Lecture/<br>Problem solving | Mid-Test1 (Week 9)/Quiz  |
| 7 | Partial ordering, partially ordered set, Hasse diagrams  | CO-II | Let $A = \{a, b, c\}$ , $P(A)$ is the power set of $A$ . Let $\subseteq$ be the inclusion relation on the elements of $P(A)$ . Draw Hasse diagram of $(P(A), \subseteq)$ .                          | Lecture/<br>Problem solving | Mid-Test1 (Week 9)/Quiz  |
| 8 | Definitions and examples of some simple algebraic systems, Definition and Examples of semigroup and monoid, general properties. Groups: Definition | CO-II | Prove that the set of idempotent elements of $M$ for any abelian monoid $M$ , $E$ forms a submonoid.  | Lecture/<br>Problem solving | Mid-Test2 (Week 10)/Quiz |
| 9 | MidExam-I  |       |   |                             |                          |

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| 10 | Basics of counting, Combinations and permutations, Enumerating Combinations and permutations with repetitions,   | CO-III | Find the number of 4 digit numbers formed by the digits 1, 2, 3, 4, 5, 6, 7 and 8 which are more than 5000, if each digit is not used more than once in a number. | Lecture/<br>Problem solving | Mid-Test2 (Week 18)/<br>Assignment (12-14) |
| 11 | Multinomial theorems, Generating Functions of sequences, Calculating coefficients  | CO-III | Find the generating function of the Fibonacci sequence.   | Lecture/<br>Problem solving | Mid-Test2 (Week 18)/<br>Assignment (12-14) |
| 12 | of Recurrence relations, generating functions, Solving Recurrence relations by substitution, generating functions and the method of characteristic roots | CO-III | Solve the recurrence $U_n - 8U_{n-1} + 21U_{n-2} - 18U_{n-3} = 0$ for $n \geq 3$ , $U_0 = 2$ ; $U_1 = 8$ , $U_2 = 31$   | Lecture/<br>Problem solving | Mid-Test2 (Week 18)/<br>Assignment (12-14) |

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|-------|--|-------|--|--|---|
| 13    | Basic concepts: Graph, Directed Graph, Multi Graph, Degree of vertex and their properties,                   | CO-IV | In every graph, show that the sum of degrees of all the vertices is twice the number of edges.   | Lecture/<br>Problem solving  | Mid-Test2 (Week18)/<br>Assignment (12-14) |
| 14    | Adjacency Matrix, Cycle Graph, Bipartite graphs, Isomorphism and Subgraphs,                                  | CO-IV | Determine whether the following graphs are isomorphic  | Lecture/<br>Problem solving  | MidTest2(Week18)/Quiz                     |
| 15    | Trees and their properties, Spanning trees: DFS, BFS, Kruskal's Algorithm for finding minimal Spanning tree. | CO-IV | Find the minimal spanning tree of the weighted graph   | Lecture/<br>Problem solving  | MidTest2(Week18)/Quiz                     |
| 16    | Introduction to Fuzzy Sets, Fuzzy Relations, Applications of Fuzzy set theory                                | CO-V  | Given $U_1 = U_2 = 1+2+3, -$<br>$A_1 = .5/1 + 1./2 + .6/3$ and $A_2 = 1./1 + .6/2$ , Find $A_1 \cap A_2$   |  | MidTest2(Week18)/Quiz                     |
| 17    | Possibility theory, Possibility-Probability relationship   | CO-V  | Show that the fuzzy set A defined over $\mathbb{R}$ with membership function<br>$\mu_A(x) = \begin{cases} 0 & x < 0 \\ \frac{x}{2} & 0 \leq x < 2 \\ 1 & 2 \leq x < 4 \\ \frac{4-x}{2} & 4 \leq x < 6 \\ 0 & x \geq 6 \end{cases}$ is convex | $\mu_A(x) = \begin{cases} 0 & x < 0 \\ \frac{x}{2} & 0 \leq x < 2 \\ 1 & 2 \leq x < 4 \\ \frac{4-x}{2} & 4 \leq x < 6 \\ 0 & x \geq 6 \end{cases}$ , | Mid-Test2 (Week18)                        |
| 18    | MidExam-II   |       |  |  |   |
| 19/20 | END EXAM   |       |  |  |   |